

# A Theoretical and Empirical Study of EFSM Dependence

Kelly Androutsopoulos<sup>1</sup>, Nicolas Gold<sup>1</sup>, Mark Harman<sup>1</sup>,

Zheng Li<sup>1</sup> and Laurence Tratt<sup>2</sup>



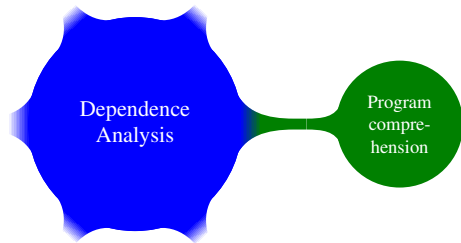
**Centre for Research in Evolution,  
Search & Testing**

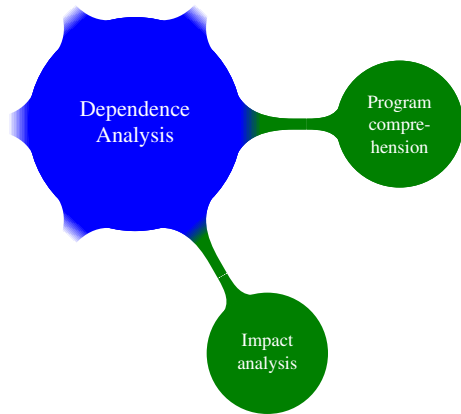
<sup>1</sup>CREST, King's College London

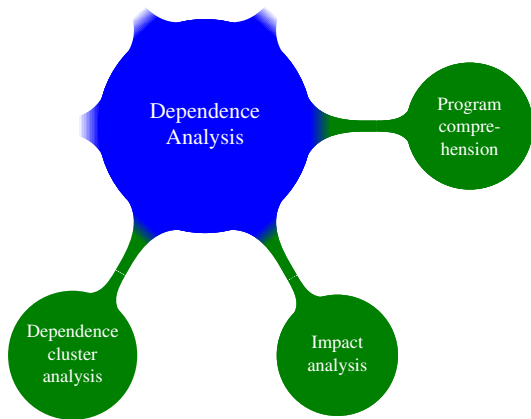
<sup>2</sup>Bournemouth University

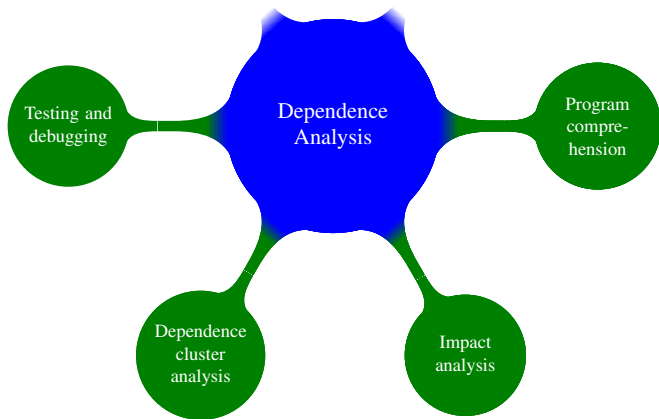


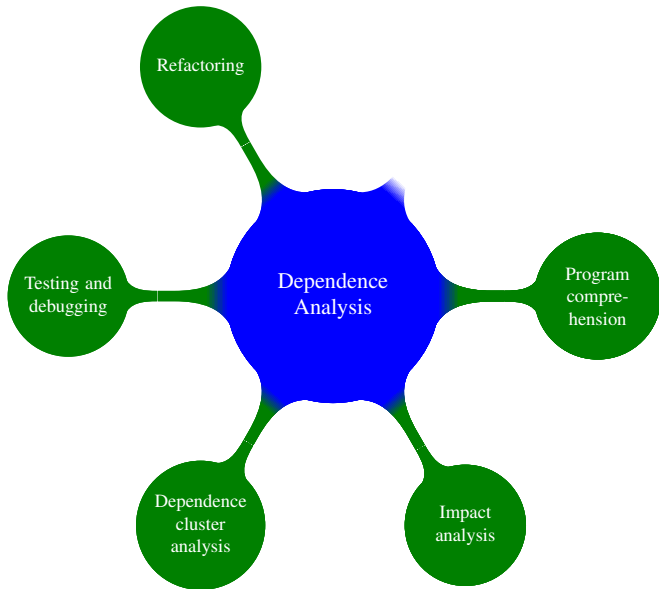
Dependence  
Analysis

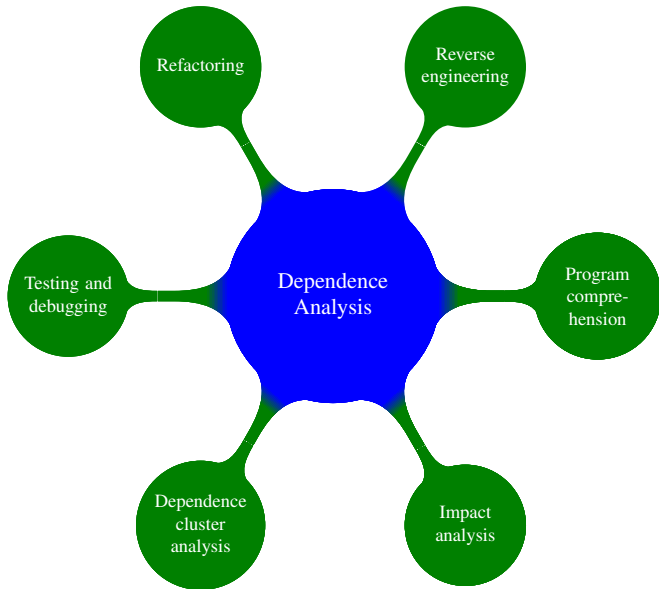




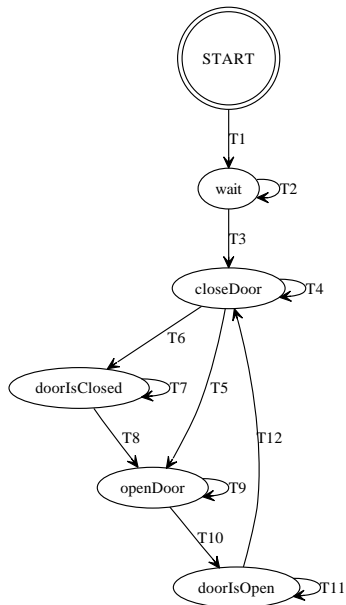


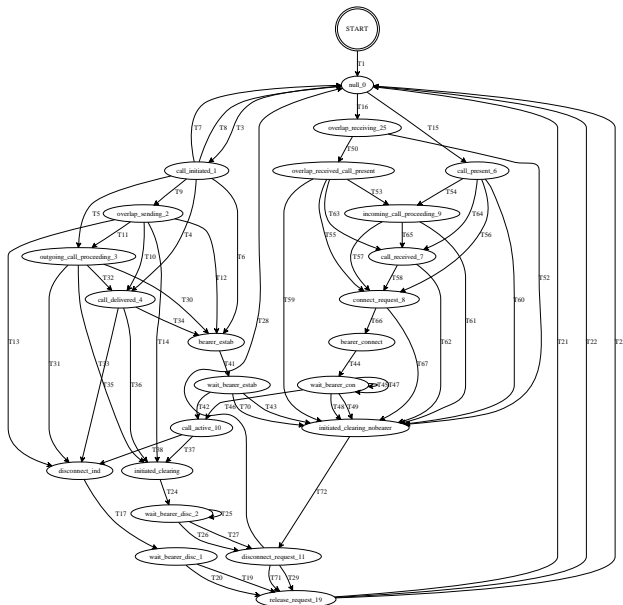




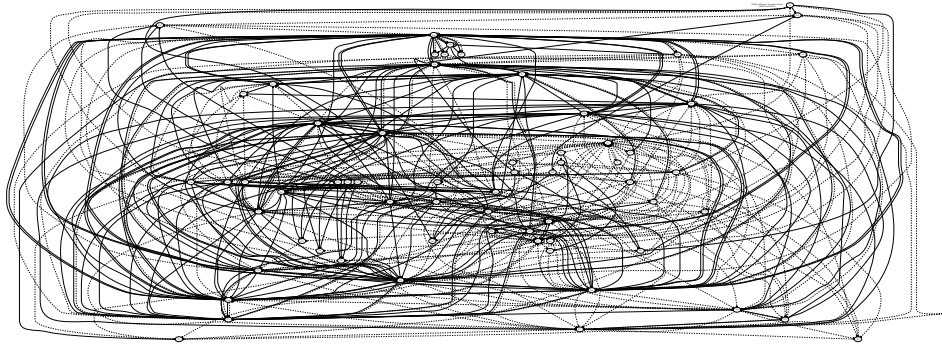








If the model like this?



## Motivation

- Models tend to be larger and more complex.

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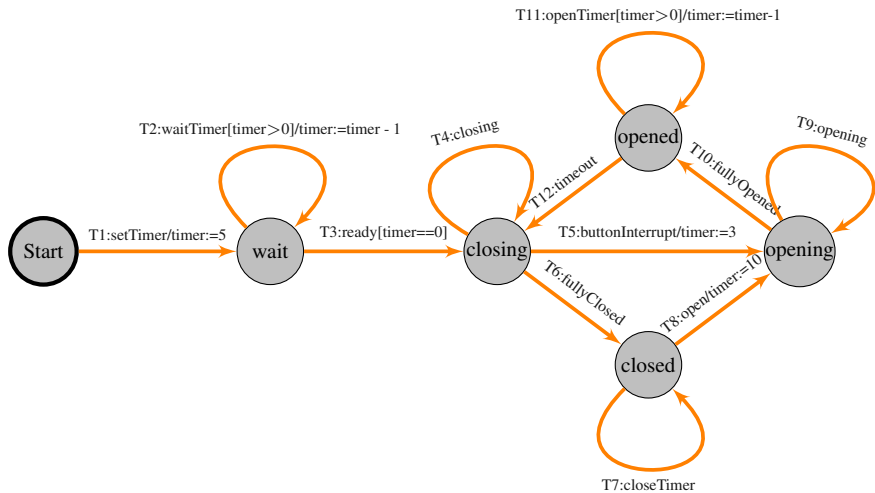
- Models tend to be larger and more complex.
- Dependence analysis has provided a valuable suite of maintenance techniques at the implementation level, but little at model level.

## Definition

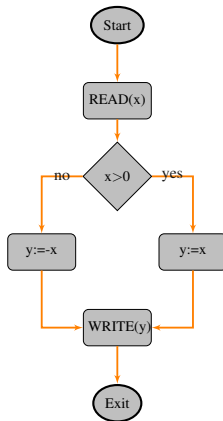
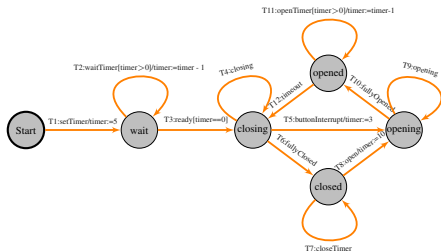
An **Extended Finite State Machine (EFSM)**  $M$  is a tuple  $(S, T, E, V)$  where  $S$  is a set of states,  $T$  is a set of transitions,  $E$  is a set of events, and  $V$  is a store represented by a set of variables. Transitions have a source state  $source(t) \in S$ , a target state  $target(t) \in S$  and a label  $lbl(t)$ . Transition labels are of the form  $e_1[c]/a$  where  $e_1 \in E$ ,  $c$  is a condition and  $a$  a sequence of actions.



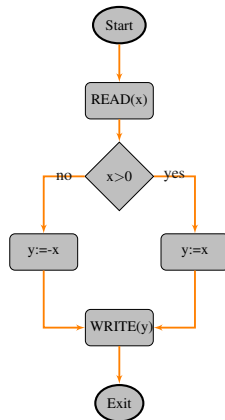
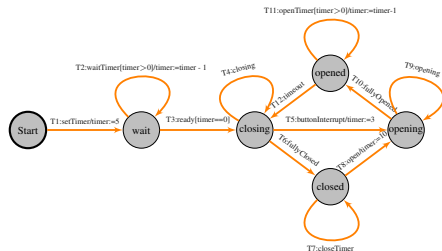
# An EFSM example: DoorControl



# EFSM VS CFG

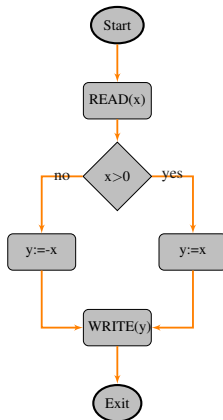
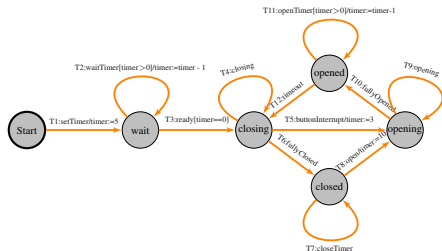






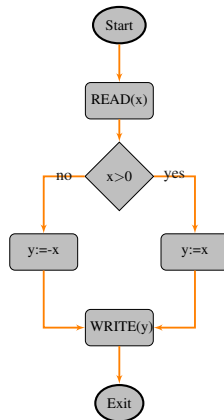
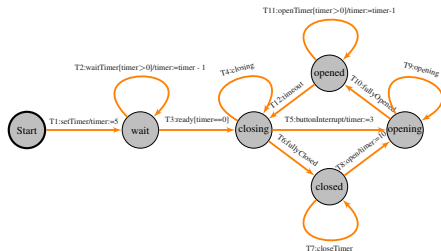
## Difference

- 1 **Transition** in EFSM VS **Node** in CFG



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- 2 Self-looping edge and multi-edges between two nodes



## Difference

- ① **Transition** in EFSM VS **Node** in CFG
- ② Self-looping edge and multi-edges between two nodes
- ③ Exit node

- Data Dependence
- Control Dependence

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  - Traditional Control Dependence [Korel et al, ICSM 2003]

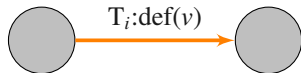
- Data Dependence
- Control Dependence
  - Traditional Control Dependence [Korel et al, ICSM 2003]
  - Non-Termination Insensitive Control Dependence (NTICD) [Ranganath et al. ESOP 2005]
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  - Non-Termination Insensitive Control Dependence (**NTICD**) [Ranganath et al. ESOP 2005]
  - Non-Termination Sensitive Control Dependence (**NTSCD**) [Ranganath et al. ESOP 2005]
  - Unfair Non-Termination Insensitive Control Dependence (**UNTICD**) [Androutsopoulos et al. FASE 2009]

## Definition

$T_i \xrightarrow{DD} T_j$  means that transitions  $T_i$  and  $T_j$  are data dependent with respect to a variable  $v$  if:

- 1  $v \in D(T_i)$ , where  $D(T_i)$  is a set of variables defined by transition  $T_i$ , i.e. variables defined by actions and by the event of  $T_i$ ;

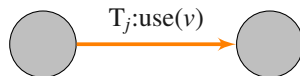
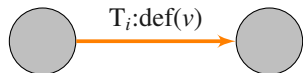




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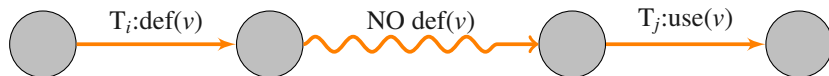
- 1  $v \in D(T_i)$ , where  $D(T_i)$  is a set of variables defined by transition  $T_i$ , i.e. variables defined by actions and by the event of  $T_i$ ;
- 2  $v \in U(T_j)$ , where  $U(T_j)$  is a set of variables used in a condition and actions of transition  $T_j$ ;



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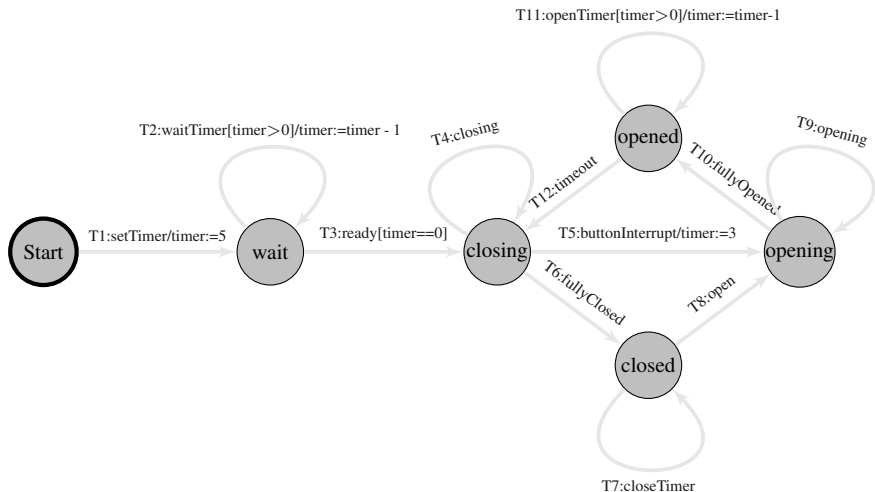
- 1  $v \in D(T_i)$ , where  $D(T_i)$  is a set of variables defined by transition  $T_i$ , i.e. variables defined by actions and by the event of  $T_i$ ;
- 2  $v \in U(T_j)$ , where  $U(T_j)$  is a set of variables used in a condition and actions of transition  $T_j$ ;
- 3 there exists a path in an EFSM from the *source*( $T_i$ ) to the *target*( $T_j$ ) whereby  $v$  is not modified by any of the intermediate transitions.



<b>Name</b>		<b>Path type</b>
NTSCD	→	Maximal Path
NTICD	→	Sink-bounded Path
UNTICD	→	Unfair Sink-bounded Path

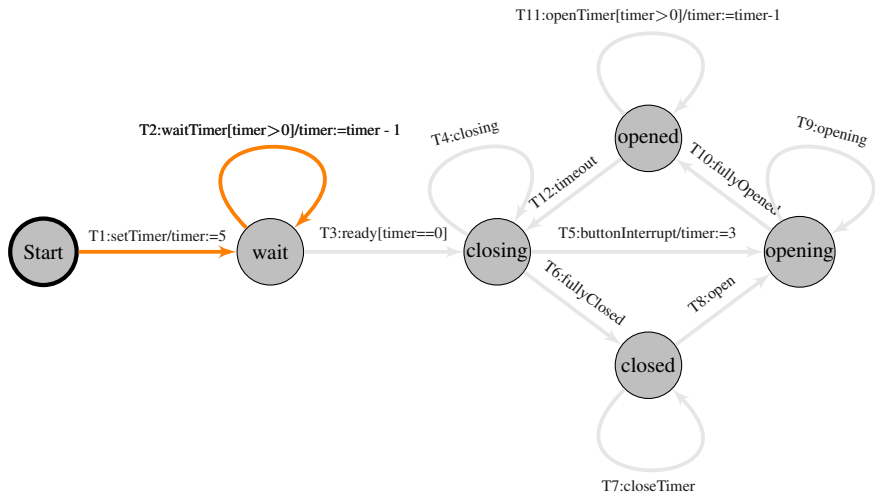
## Definition (Maximal Path)

A **maximal path** is any path that terminates in a final transition, or is infinite.



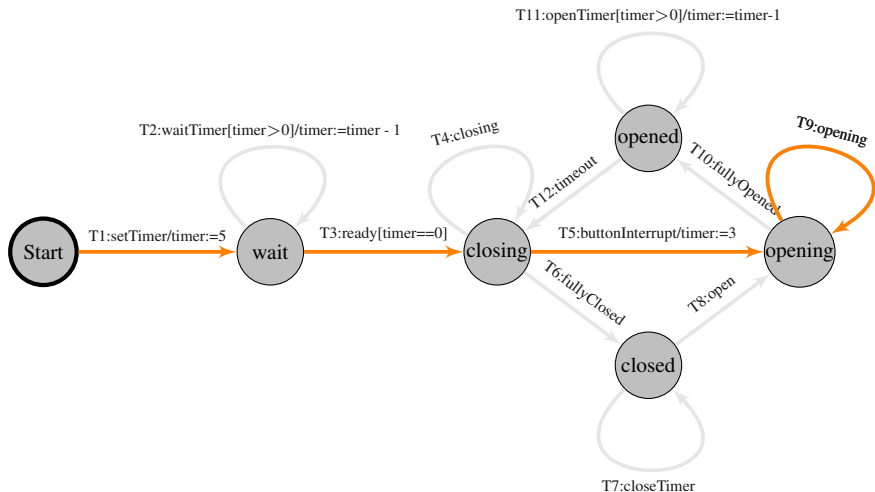
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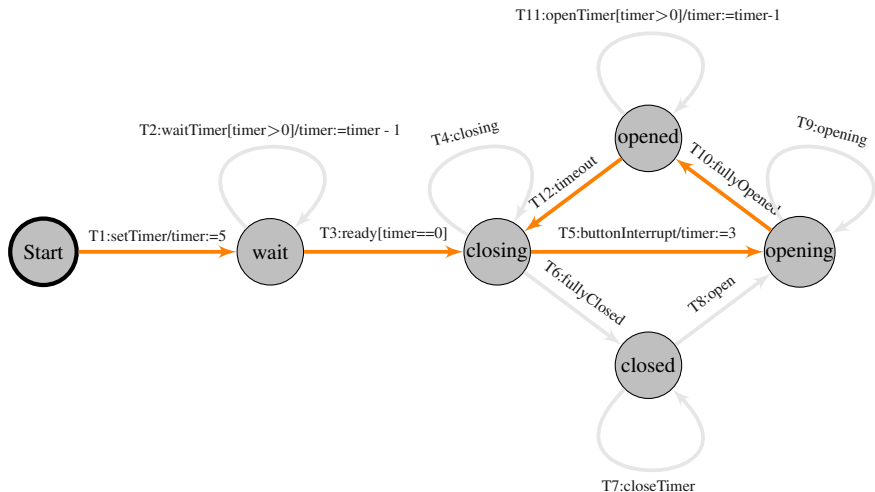
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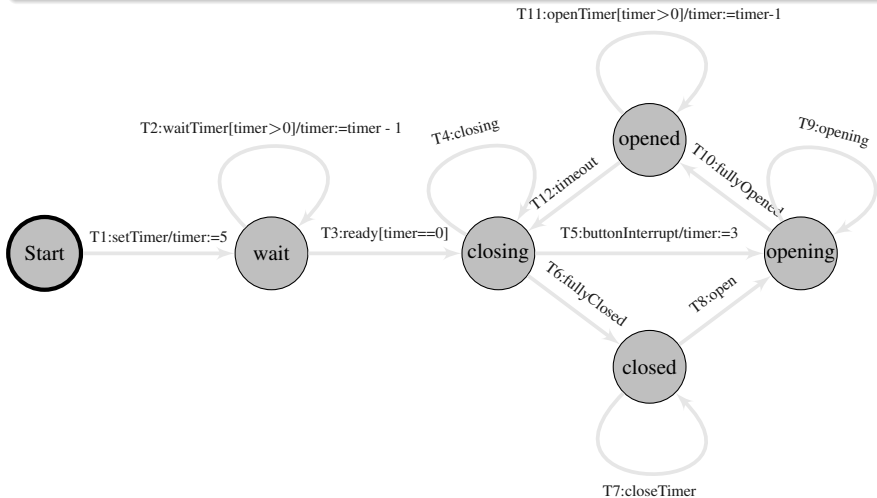
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## Definition (Control Sink)

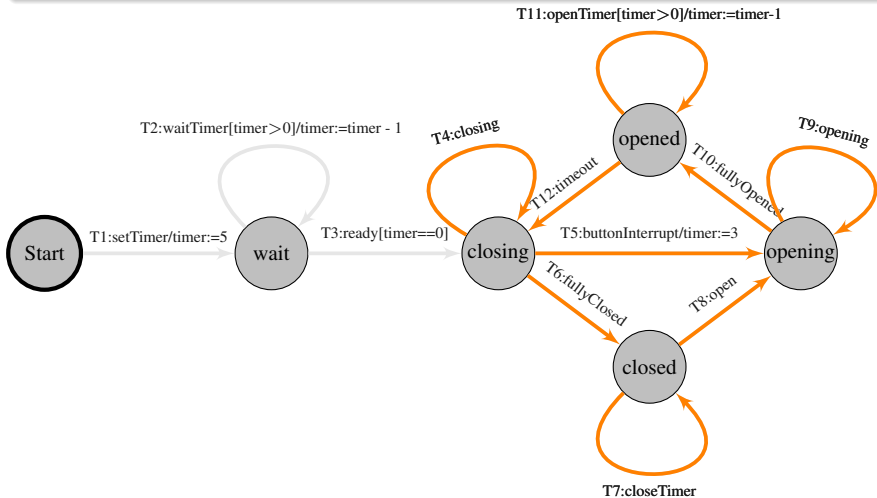
A **control sink** in an EFSM is a set of transitions  $\mathcal{K}$  that form a strongly connected component (SCC) such that, for each transition  $t$  in  $\mathcal{K}$  each successor of  $t$  is also in  $\mathcal{K}$ .





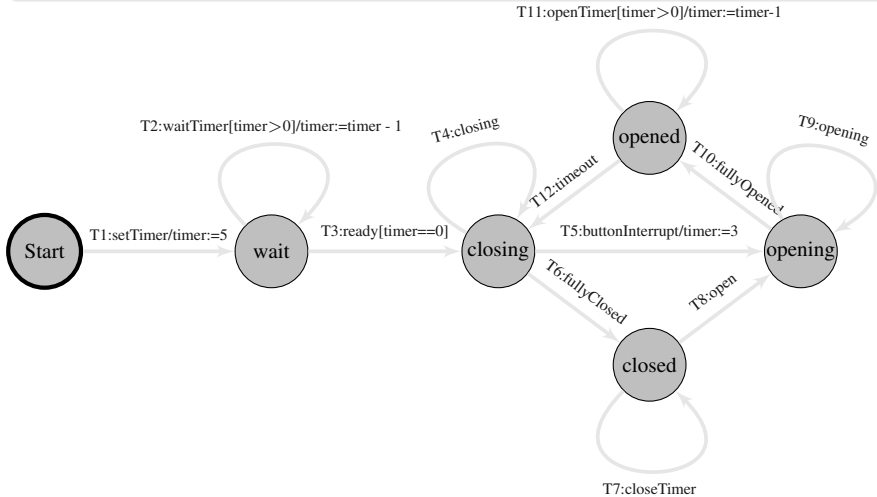
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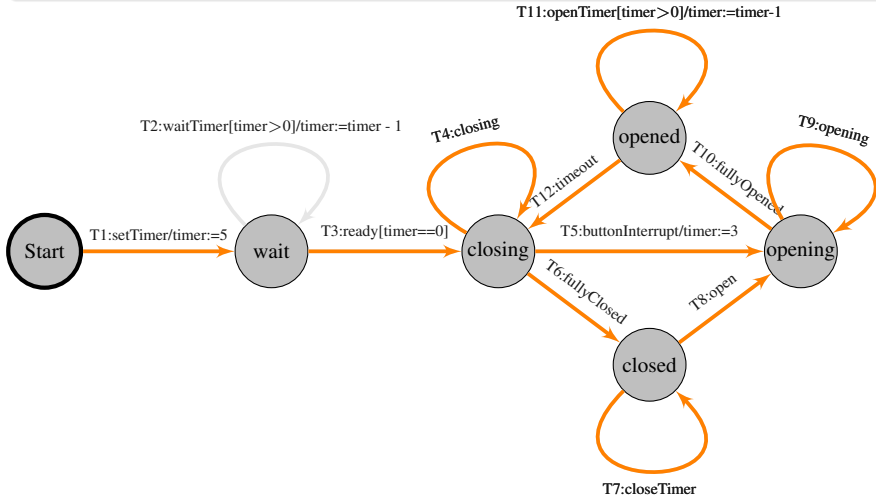
## Definition (Sink-bounded Paths)

A maximal path  $\pi$  is **sink-bounded** iff (i) there exists a control sink  $\mathcal{K}$  such that  $\mathcal{K} \cap \pi \neq \emptyset$  and, (ii) if  $\pi$  is infinite, then all transitions in  $\mathcal{K}$  occur infinitely often.



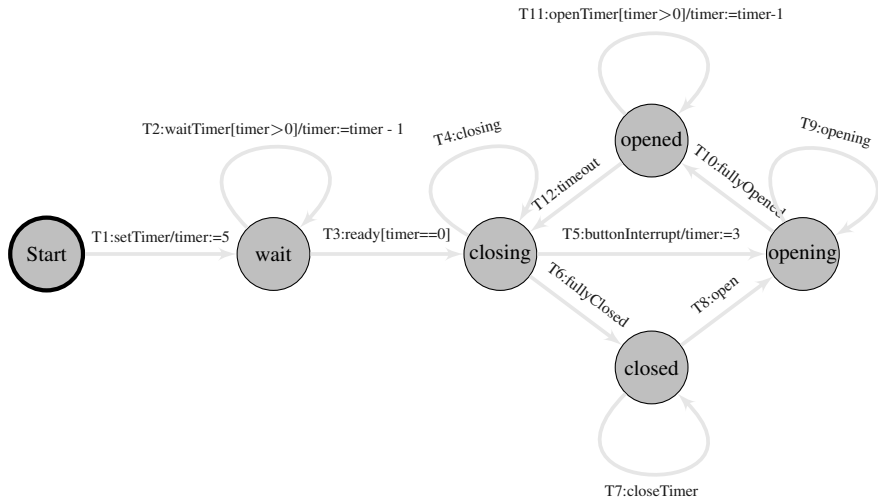
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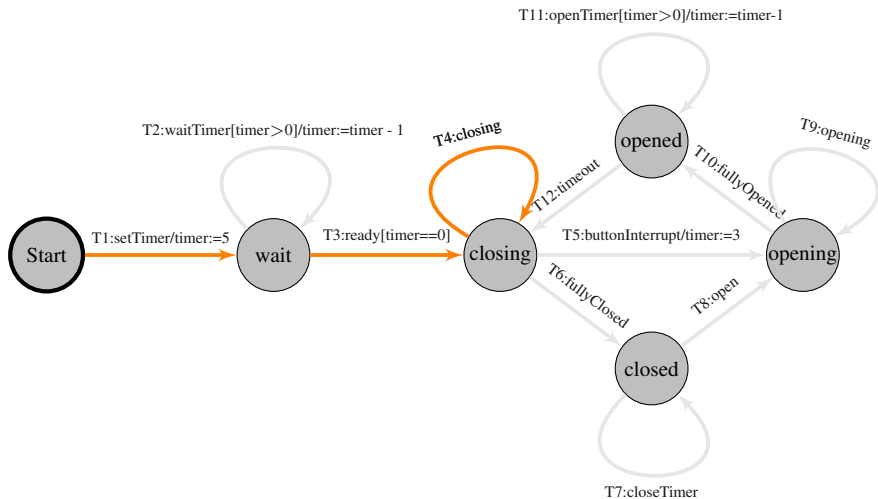
## Definition (Unfair Sink-bounded Paths)

A maximal path  $\pi$  is **unfair sink-bounded** iff there exists a control sink  $\mathcal{K}$  such that:  $\pi$  contains a transition from  $\mathcal{K}$ .



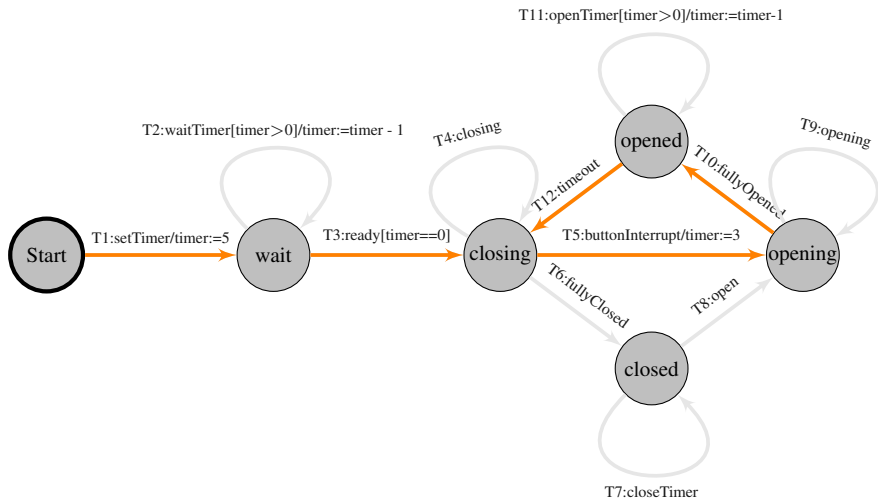
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## Definition (Control Dependence)

$T_i \xrightarrow{\text{CD}} T_j$  means that a transition  $T_j$  is control dependent on a transition  $T_i$  iff  $T_i$  has at least one sibling  $T_k$  such that:

- 1 for all paths  $\pi \in \text{PATHs}(\text{target}(T_i))$ , the  $\text{source}(T_j)$  belongs to  $\pi$ ;
- 2 there exists a path  $\pi \in \text{PATHs}(\text{source}(T_k))$  such that the  $\text{source}(T_j)$  does not belong to  $\pi$ .

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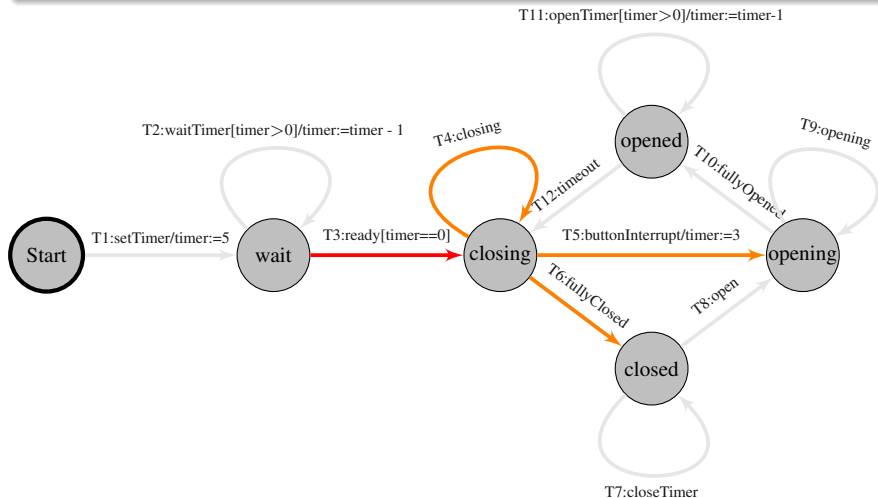
- 1 for all paths  $\pi \in \text{PATHs}(target(T_i))$ , the  $source(T_j)$  belongs to  $\pi$ ;
- 2 there exists a path  $\pi \in \text{PATHs}(source(T_k))$  such that the  $source(T_j)$  does not belong to  $\pi$ .

CD		PATH type
NTSCD	→	Maximal Path
NTICD	→	Sink-bounded Path
UNTICD	→	Unfair Sink-bounded Path



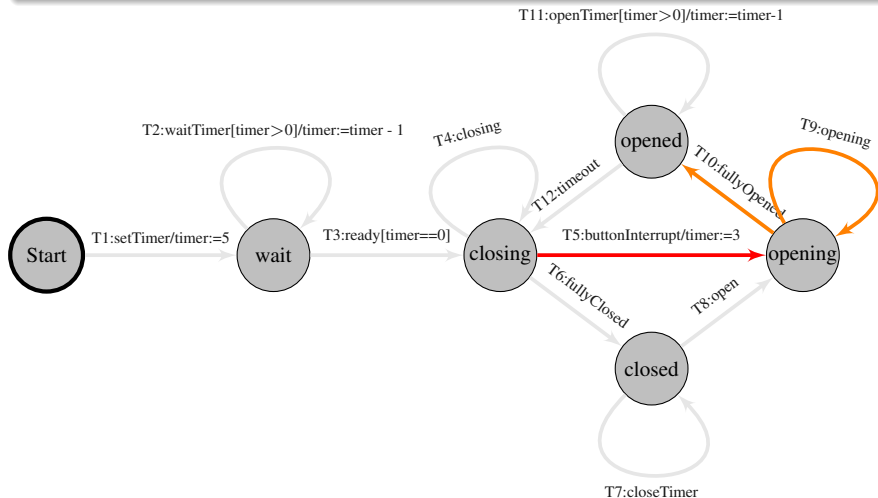
## Example (NTSCD)

- $T_3 \xrightarrow{\text{NTSCD}} T_4, T_5, T_6$
- $T_5 \xrightarrow{\text{NTSCD}} T_9, T_{10}$



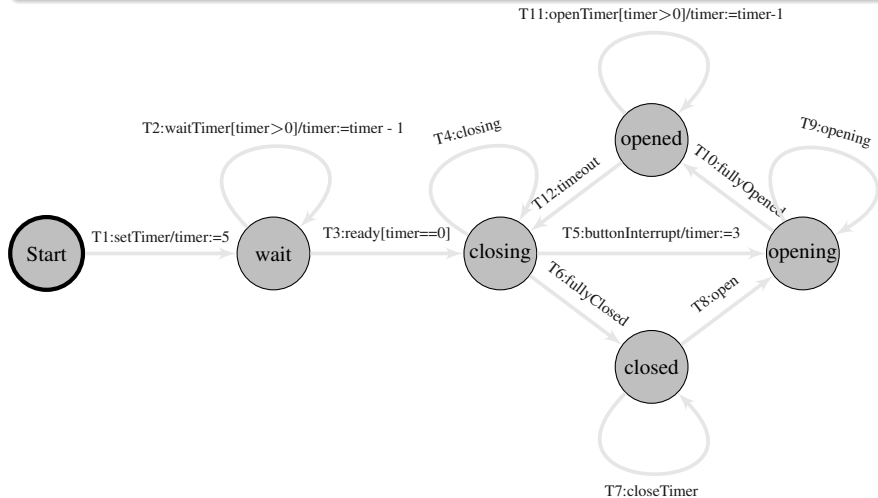
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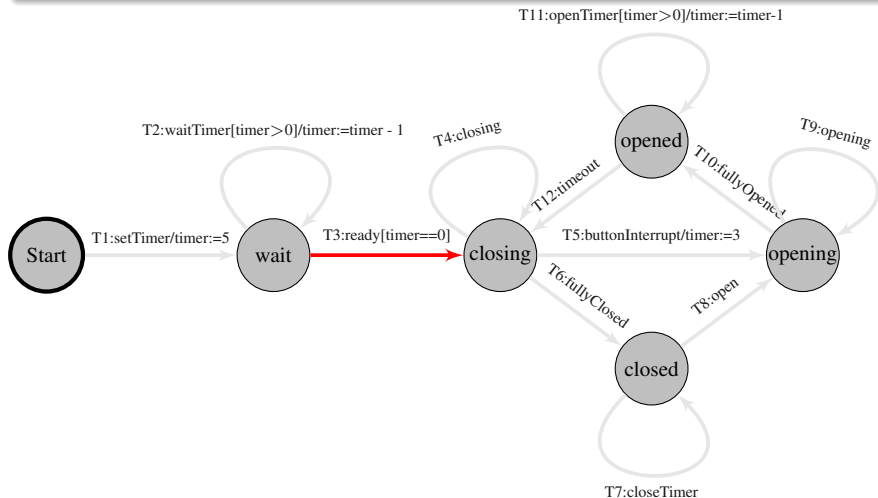
## Example (NTICD)

NO NTICD in this example



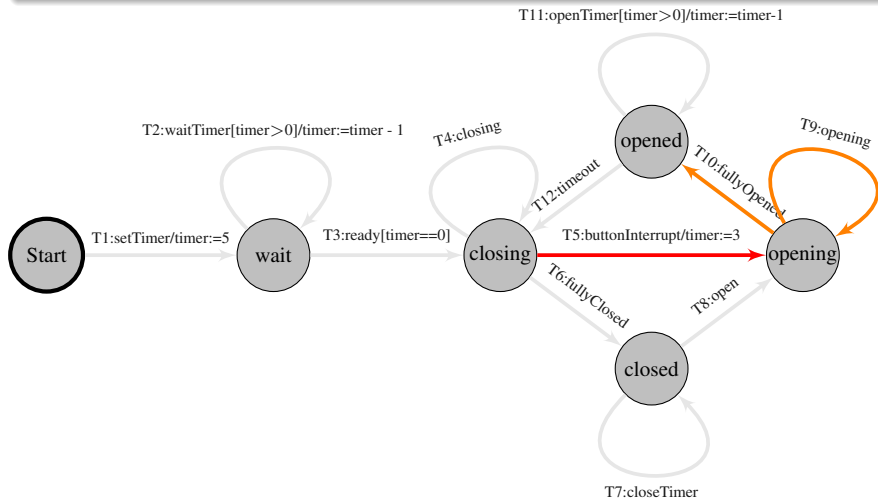
# Example (UNTICD)

- $T_3 \xrightarrow{\text{UNTICD}}$
- $T_5 \xrightarrow{\text{UNTICD}} T_9, T_{10}$



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## Definition (Slice Criterion)

A slicing criterion is a pair  $(t, v)$  where transition  $t \in T$  and variable set  $v \subseteq V$ .

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## Definition (Slice)

A slice of an EFSM  $M$ , is another EFSM  $M'$ , whose transitions will be directly or indirectly (transitive closure) data and control dependent on the slicing criterion  $c$ .

### Definition (Slice Size)

For a model  $M$ ,  $t'$  is a transition dependent on  $t$  (i.e.,  $t' \in T \wedge t \rightarrow t'$ ), the size of slice with respect to  $t$  is:

$$|\mathcal{S}(M, t)| = \frac{\sum t'}{|M|}$$



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$$|\mathcal{S}(M, t)| = \frac{\sum t'}{|M|}$$

### Definition (Average Slice Size)

For a model  $M$ ,  $NT$  is subset of transitions of  $M$  with non-zero slice size (i.e.,  $NT \subseteq T$  and  $\forall t \in NT, |\mathcal{S}(M, t)| > 0$ ). Thus, the average slice size of  $M$  is:

$$\text{Avg}(M) = \frac{\sum_{t \in NT} |\mathcal{S}(M, t)|}{|NT|}$$

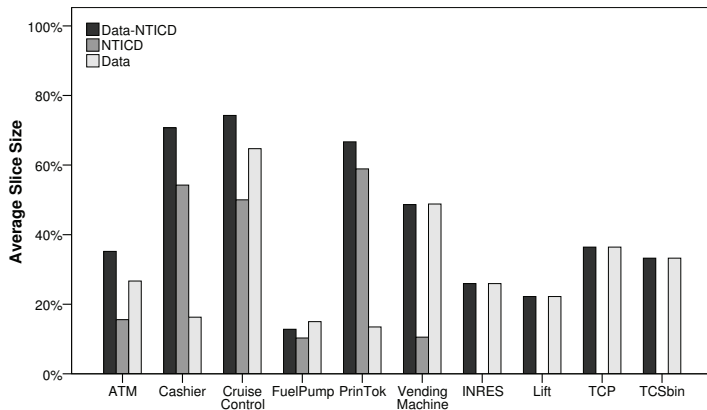
Models	#S	#T	#V	EXIT	Description
ATM	9	23	8	Yes	Automated Teller Machine
Cashier	12	21	10	Yes	Cashier Machine
CruiseControl	5	17	18	Yes	Cruise Control System
FuelPump	13	25	12	Yes	Fuel Pump System
PrinTok	11	89	5	Yes	Print Token
VendingMachine	7	28	7	Yes	Vending Machine system
INRES	8	18	8	No	INRES protocol
TCP	12	57	31	No	TCP Standard(RFC793)
TCSbin	24	65	61	No	Telephony Control Protocol
Lift	6	12	1	No	Lift System
<b>Total</b>	107	355	161		

Dependence	Forward Slices		Backward Slices	
	# T	Avg	# T	Avg
DD+NTSCD				
DD+NTICD				
DD+UNTICD				
DD				
NTSCD				
NTICD				
UNTICD				

Dependence	Forward Slices		Backward Slices	
	# T	Avg	# T	Avg
DD+NTSCD	276	87.45%		
DD+NTICD	220	61.99%		
DD+UNTICD	267	83.20%		
DD	161	35.67%		
NTSCD	205	86.10%		
NTICD	92	78.67%		
UNTICD	190	82.21%		

Dependence	Forward Slices		Backward Slices	
	# T	Avg	# T	Avg
DD+NTSCD	276	87.45%	345	70.46%
DD+NTICD	220	61.99%	278	49.48%
DD+UNTICD	267	83.20%	335	66.83%
DD	161	35.67%	174	33.15%
NTSCD	205	86.10%	336	53.63%
NTICD	92	78.67%	167	44.59%
UNTICD	190	82.21%	313	51.00%

# Backward Slice size using NTICD



# Correlation of Slice Size

Model	Dependence	Forward			Backward		
		NTICD	UNTICD	NTSCD	NTICD	UNTICD	NTSCD
ATM	NTICD	-	1.000	.652	-	1.000	.941
	UNTICD	1.000	-	.652	1.000	-	.941
	NTSCD	.652	.652	-	.941	.941	-
Cashier	NTICD	-	1.000	.898	-	1.000	1.000
	UNTICD	1.000	-	.898	1.000	-	1.000
	NTSCD	.898	.898	-	1.000	1.000	-
CruiseControl	NTICD	-	1.000	1.000	-	1.000	1.000
	UNTICD	1.000	-	1.000	1.000	-	1.000
	NTSCD	1.000	1.000	-	1.000	1.000	-
FuelPump	NTICD	-	1.000	.786	-	1.000	-.509
	UNTICD	1.000	-	.786	1.000	-	-.509
	NTSCD	.786	.786	-	-.509	-.509	-
PrinTok	NTICD	-	1.000	1.000	-	1.000	1.000
	UNTICD	1.000	-	1.000	1.000	-	1.000
	NTSCD	1.000	1.000	-	1.000	1.000	-
VendingMachine	NTICD	-	1.000	.360	-	1.000	.224
	UNTICD	1.000	-	.360	1.000	-	.224
	NTSCD	.360	.360	-	.224	.224	-
INRES	NTICD	-	x	x	-	x	x
	UNTICD	x	-	1.000	x	-	1.000
	NTSCD	x	1.000	-	x	1.000	-
Lift	NTICD	-	x	x	-	x	x
	UNTICD	x	-	.813	x	-	1.000
	NTSCD	x	.813	-	x	1.000	-
TCP	NTICD	-	x	x	-	x	x
	UNTICD	x	-	1.000	x	-	1.000
	NTSCD	x	.	-	x	1.000	-
TCSbin	NTICD	-	x	x	-	x	x
	UNTICD	x	-	1.000	x	-	1.000
	NTSCD	x	1.000	-	x	1.000	-

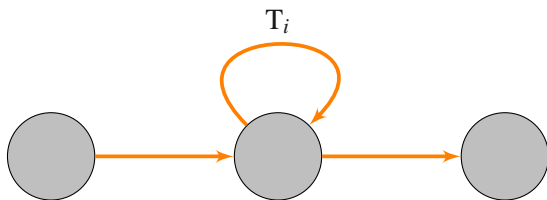
# Correlation of Slice Size

Model	Dependence	Forward			Backward		
		NTICD	UNTICD	NTSCD	NTICD	UNTICD	NTSCD
ATM	NTICD	-	1.000	.652	-	1.000	.941
	UNTICD	1.000	-	.652	1.000	-	.941
	NTSCD	.652	.652	-	.941	.941	-
Cashier	NTICD	-	1.000	.898	-	1.000	1.000
	UNTICD	1.000	-	.898	1.000	-	1.000
	NTSCD	.898	.898	-	1.000	1.000	-
CruiseControl	NTICD	-	1.000	1.000	-	1.000	1.000
	UNTICD	1.000	-	1.000	1.000	-	1.000
	NTSCD	1.000	1.000	-	1.000	1.000	-
FuelPump	NTICD	-	1.000	.786	-	1.000	-.509
	UNTICD	1.000	-	.786	1.000	-	-.509
	NTSCD	.786	.786	-	-.509	-.509	-
PrinTok	NTICD	-	1.000	1.000	-	1.000	1.000
	UNTICD	1.000	-	1.000	1.000	-	1.000
	NTSCD	1.000	1.000	-	1.000	1.000	-
VendingMachine	NTICD	-	1.000	.360	-	1.000	.224
	UNTICD	1.000	-	.360	1.000	-	.224
	NTSCD	.360	.360	-	.224	.224	-
INRES	NTICD	-	x	x	-	x	x
	UNTICD	x	-	1.000	x	-	1.000
	NTSCD	x	1.000	-	x	1.000	-
Lift	NTICD	-	x	x	-	x	x
	UNTICD	x	-	.813	x	-	1.000
	NTSCD	x	.813	-	x	1.000	-
TCP	NTICD	-	x	x	-	x	x
	UNTICD	x	-	1.000	x	-	1.000
	NTSCD	x	.	-	x	1.000	-
TCSbin	NTICD	-	x	x	-	x	x
	UNTICD	x	-	1.000	x	-	1.000
	NTSCD	x	1.000	-	x	1.000	-



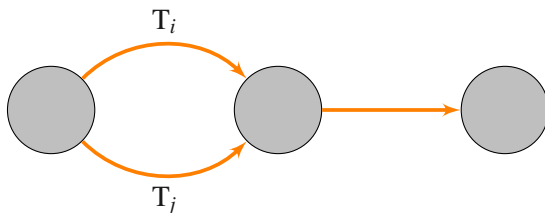
## Proposition

For an EFSM  $M$ , if  $T_i \in M$  is a self-looping transition, then there is no transition  $T_j$  that is control dependent (NTSCD, NTICD or UNTICD) on  $T_i$ .



## Proposition

For an EFSM  $M$ , if two transitions  $T_i$  and  $T_j$  have the same source and target states, and  $T_i \xrightarrow{CD} T_l$  (using NTSCD, NTICD or UNTICD) then  $T_j \xrightarrow{CD} T_l$  (using NTSCD, NTICD or UNTICD respectively).



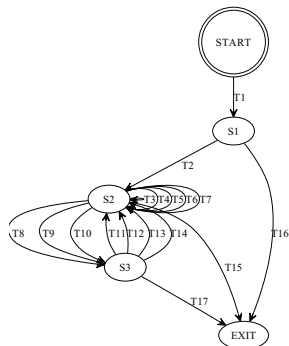
### Proposition

For an EFSM  $M$ , if  $T_i \xrightarrow{\text{CD}} T_j$  (either NTSCD, NTICD, or UNTICD),  $\text{source}(T_j)$  must belong to the **shortest path** of type PATH in  $\text{PATHs}(\text{target}(T_i))$ .

This proposition has been used to reduce the cost of computation on NTSCD, NTICD, or UNTICD.

## Proposition

For an EFSM  $M$ , if all states  $s \in M$  where  $s \neq \text{START}$  have a transition  $T_i$  where  $\text{source}(T_i) = s$  and  $\text{target}(T_i) = \text{EXIT}$ , then the set of transitions that are directly control dependent on  $T_i$  are the same for all types of control dependence, i.e. NTSCD, NTICD and UNTICD.



# Question?

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### Conclusion

- We empirically studied slice size for EFSM using 10 benchmark examples and real world production EFSM models. The results reveal that current definitions of dependence lead to slice sizes that are notably larger than the existing benchmark data for program slice size.
- Forward slice sizes tend to be larger than backward slice size for EFSMs.
- Four of the novel findings arising from the empirical results are formalised and proved.

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- Forward slice sizes tend to be larger than backward slice size for EFSMs.
- Four of the novel findings arising from the empirical results are formalised and proved.

### Future Work

- Weak Order Dependence(WOD)
- Slicing algorithm